

國立台灣科技大學九十七學年度碩士班招生試題

系所組別： 自動化及控制研究所碩士班甲組、乙組

科 目： 工程數學

總分為100分，題號請標示清楚。

1. Solve the following differential equations:

(1) $yy' + 2t + y^2 = 0; \quad y(0) = 2 \quad (10\%)$

(2) $y'' - y = 5\sin^2(t); \quad y(0) = 2, y'(0) = -4 \quad (10\%)$

2. Solve $x(t)$ and $y(t)$ from the simultaneous differential equations. (15%)

$x' - x + y = e^{-t}$

$y' - 2x + 2y = e^{-t} \sin(2t)$

3. Solve the following equation by using Laplace Transform method. (15%)

$y' + 3y + 2 \int_0^t y dt = H(t - 2)$

where $y(0) = 1$ and $H(t) = \begin{cases} 0 & t < 0 \\ 1 & t \geq 0 \end{cases}$

4. Determine eigenvalues and eigenvectors of A (20%)

$$A = \begin{bmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{bmatrix}$$

5. Find $\int_0^{2\pi} \frac{d\theta}{3 - 2\cos\theta + \sin\theta}$ (10%)

6. Solve the P.D.E. $\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = 0$ with the following boundary conditions:

$\phi(0, y) = 0$

$\phi(h, y) = 0 \quad (20\%)$

$\phi(x, 0) = g(x)$

$\phi(x, l) = 0$

