

## 國立台灣科技大學九十七學年度碩士班招生試題

系所組別：電機工程系碩士班己組

科目：工程數學

總分 100 分

(1) Find a unit normal vector  $\mathbf{n}$  on the plane  $4x^2 + y^2 = z$  at the point  $(1, -2, 8)$ . (16%)(2) Evaluate the integral  $\oint_C \frac{1}{z^2(z-2i)} dz$  where C is (a)  $|z-1|=1$ , (b)  $|z-1|=2$ , (c)  $|z-1|=3$ . (18%)(3) Find the probability of  $P(x > V)$  for a Rayleigh distribution

$$p(x) = \frac{x}{\psi^2} e^{-x^2/2\psi^2}, x \geq 0. (16\%)$$

(4) Given  $A = \begin{pmatrix} 2 & 1 & 0 & -5 \\ -1 & 0 & 1 & 2 \end{pmatrix}$ (a) Find a basis for the nullspace of  $A$ . (8%)(b) Given that  $\{(2, 1, 0, -5)^T, (-1, 2, 5, 0)^T\}$  is an orthogonal basis for the column space of  $A^T$ , find the vector in the column space of  $A^T$  that is closest to  $(-1, 0, 0, 1)^T$ . (12%)(5) Find the inverse Laplace transform of  $Y(s) = \frac{2}{s^3(s+2)^2}$ . (15%)(6) Given the Fourier transform pair:  $x(t) \leftrightarrow X(\omega)$ , derive the Fourier transform of  $x(at)$ . Also find  $X(\omega)$  when  $x(t) = e^{-ct}$  where  $c > 0$ . (15%)